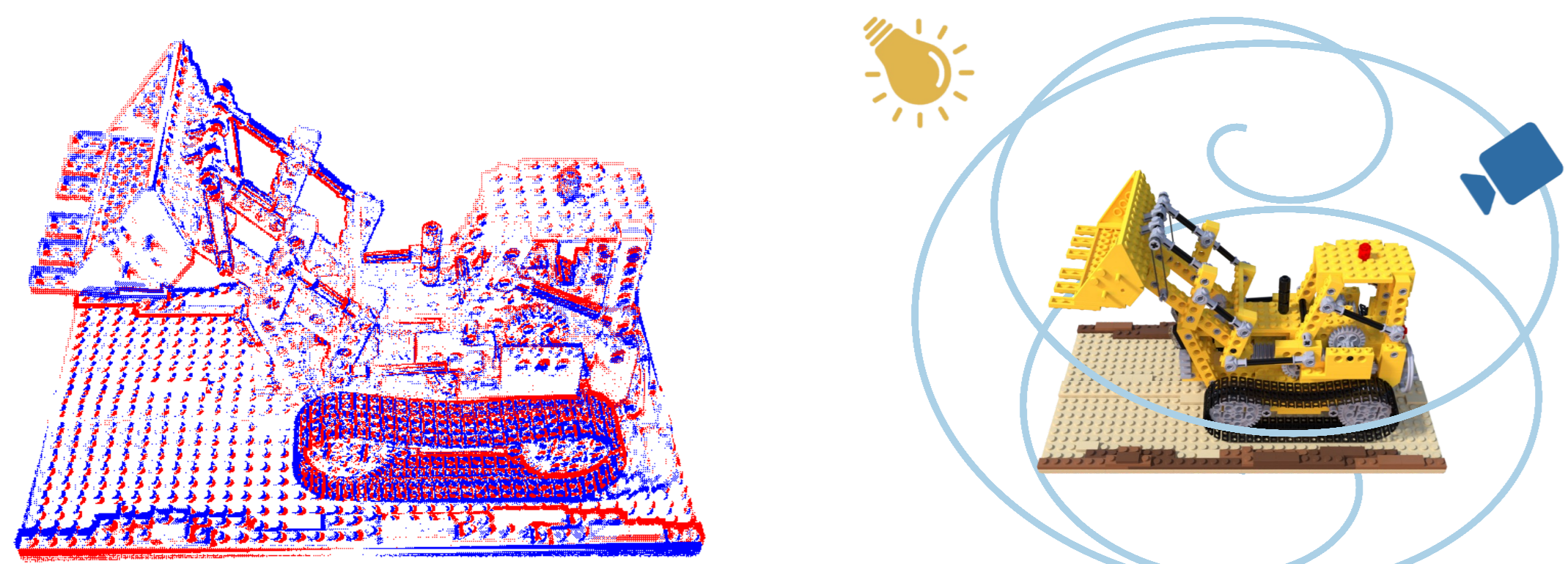
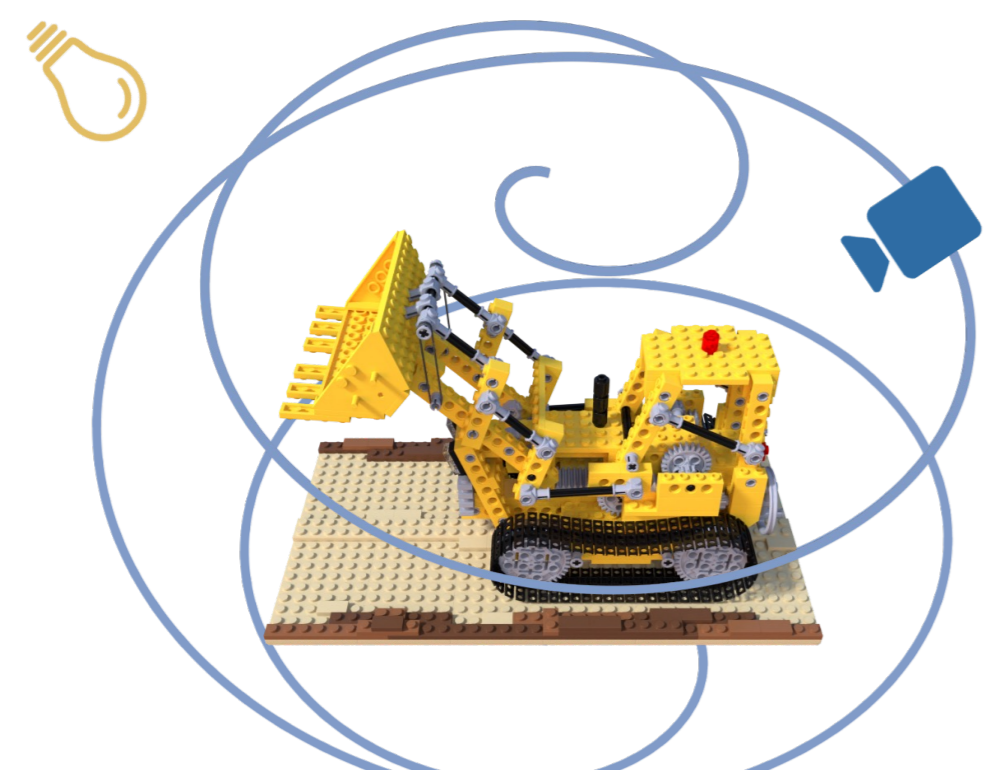
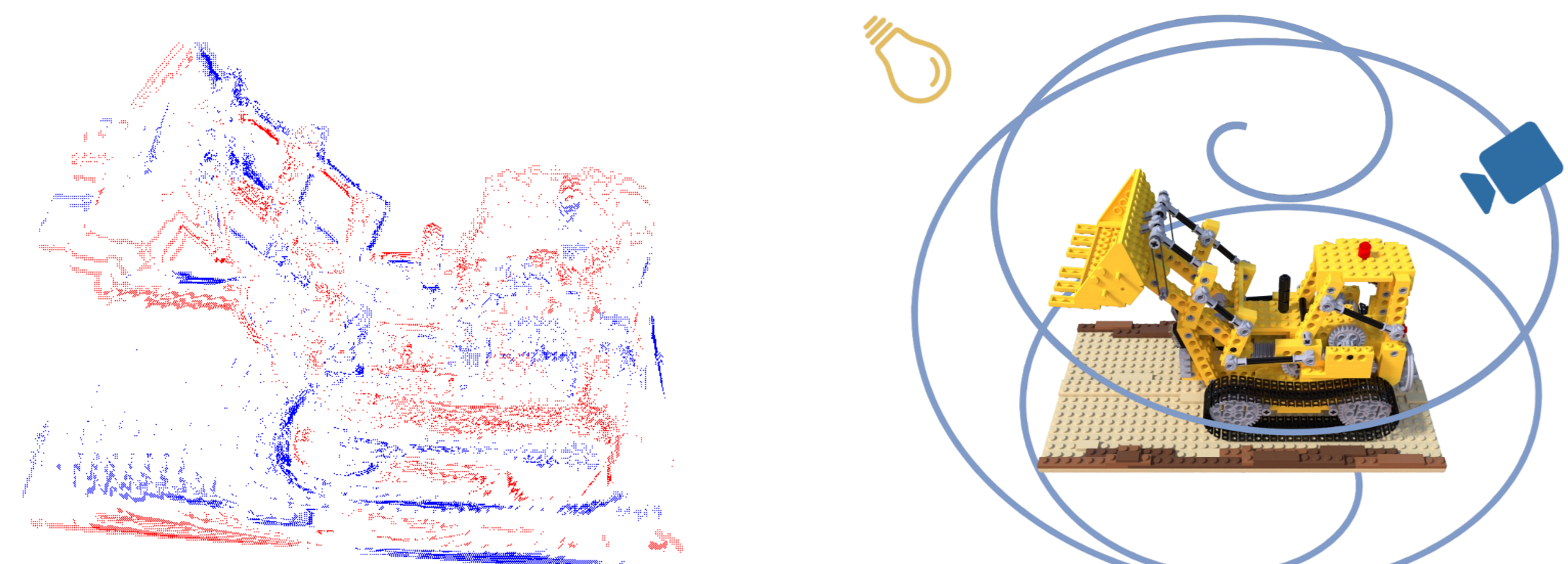


Motivation

- Event cameras outperform standard cameras under:
 - ❖ High speed
 - ❖ High dynamic range
 - ❖ Low light
 due to their distinctive principle of operation
- However, event cameras also suffer from motion blur, especially under these challenging conditions
- This is due to the limited bandwidth of the event sensor pixel, which is mostly proportional to the light intensity



(a) Minimally motion-blurred events (left), under low speed and bright light (right).

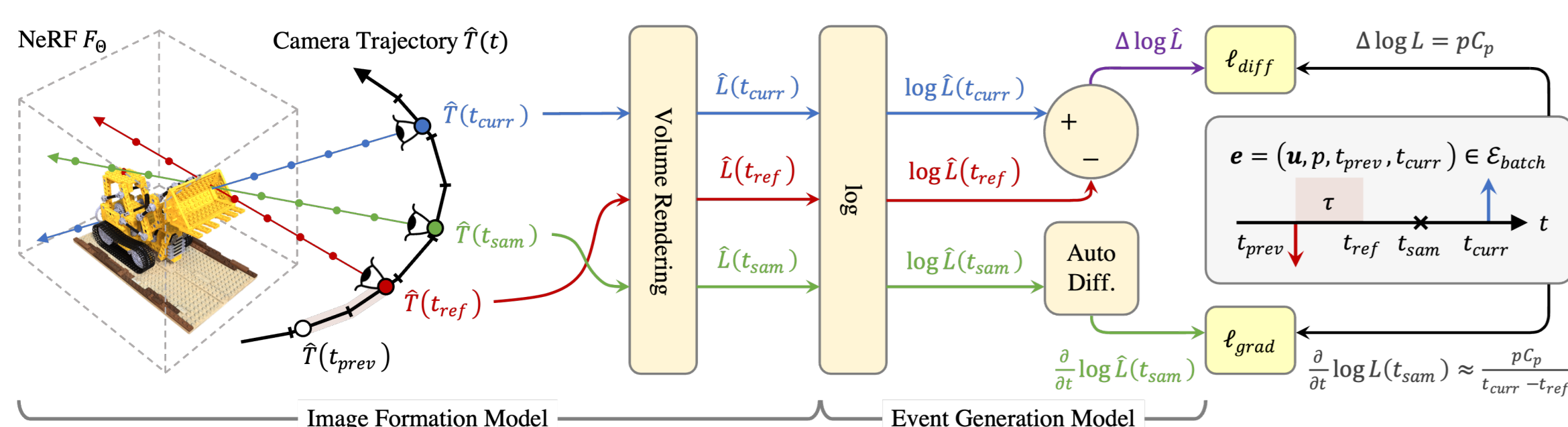


(b) Significantly motion-blurred events (left), under high speed and low light (right).

Research Question

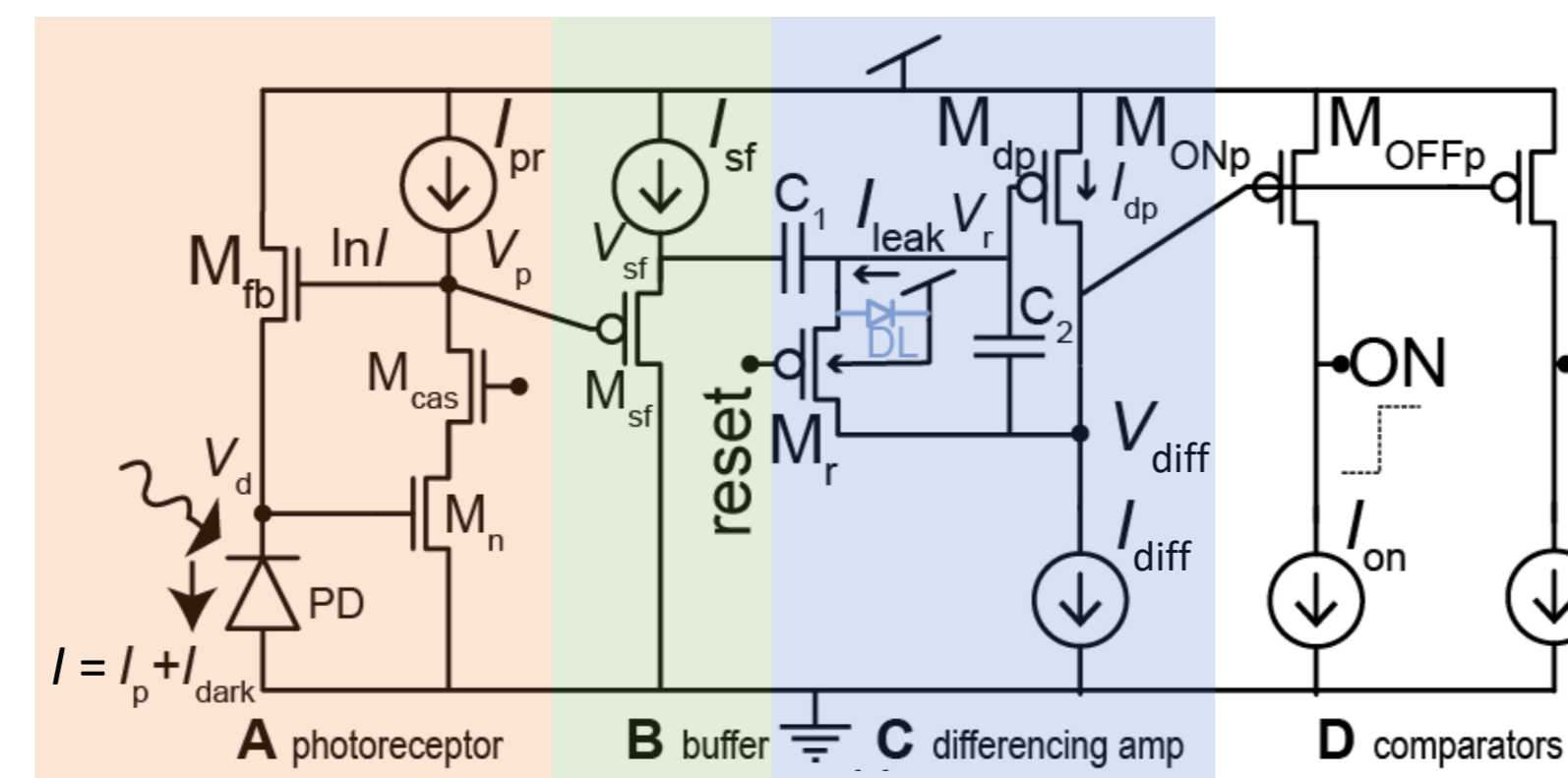
How to reconstruct blur-minimal NeRFs from motion-blurred events, generated under high-speed or low-light conditions?

Prior Work: Robust e-NeRF



Proposed Method: Deblur e-NeRF

Pixel Bandwidth Model



Input: $u = \log L$

State: $\mathbf{x} = [\partial \log L_p / \partial t \log L_p \log L_{sf} \log L_{diff}]^\top$

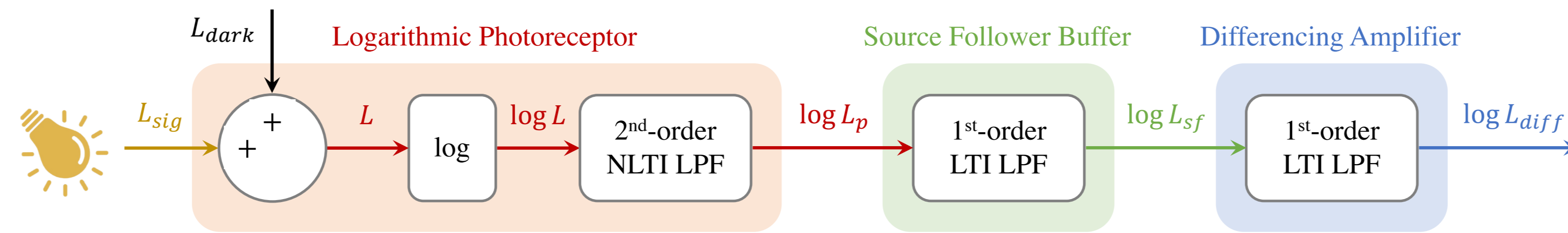
Output: $\mathbf{y} = [\log L_{sf} \log L_{diff}]^\top$

State-Space Model:

$\dot{\mathbf{x}}(t) = A(u(t)) \mathbf{x}(t) + B(u(t)) u(t)$

$\mathbf{y}(t) = C \mathbf{x}(t)$, where:

$$A(u) = \begin{bmatrix} -2\zeta(u)\omega_n(u) - \omega_n^2(u) & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & \omega_{c,sf} & -\omega_{c,sf} & 0 \\ 0 & 0 & \omega_{c,diff} & -\omega_{c,diff} \end{bmatrix}, \quad B(u) = \begin{bmatrix} \omega_n^2(u) \\ 0 \\ 0 \\ 0 \end{bmatrix}, \quad C = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Steady-State Model of Differencing Amplifier Reset Mechanism:

$$\log L_{blur}(t) = \log L_{diff}(t) + \log L_{delta}(t_{ref}) e^{-\omega_{c,diff}(t-t_{ref})}$$

where $\log L_{delta} = \log L_{sf} - \log L_{diff}$ and $t \geq t_{ref}$.

Synthesis of Motion-Blurred Effective Log-Radiance

Continuous-Time NLTI System

$$\dot{\mathbf{x}}(t) = A(t) \mathbf{x}(t) + B(t) u(t)$$

$$\mathbf{y}(t) = C \mathbf{x}(t)$$

Continuous-Time LTV System

$$\dot{\mathbf{x}}(t) = A[k] \mathbf{x}(t) + B[k] u(t)$$

$$\mathbf{y}(t) = C \mathbf{x}(t)$$

Linearize

Discretize

$$\mathbf{y}[k] \approx \sum_{i=k_0}^k \hat{\mathbf{w}}[i] u[i]$$

Discrete-Time LTV Solution

$$\mathbf{x}[k+1] = A_d[k] \mathbf{x}[k] + B_d[k] u[k] + \tilde{B}_d[k] u[k+1]$$

$$\mathbf{y}[k] = C_d \mathbf{x}[k]$$

Discrete-Time LTV System

Solve

Importance Sampling: $T_i \sim \text{Exp}(t_k - t_i; \omega_{c,dom,min}) = \omega_{c,dom,min} e^{-\omega_{c,dom,min}(t_k - t_i)}$

Threshold-Normalized Total Variation Loss

$$\ell_{tv}(e) = \left| \frac{\delta \log \hat{L}_{blur}}{\bar{C}} \right|, \quad \text{where } \bar{C} = \frac{1}{2}(C_{-1} + C_{+1}),$$

$$\delta \log \hat{L}_{blur} := \log \hat{L}_{blur}(\mathbf{u}, t_{end}) - \log \hat{L}_{blur}(\mathbf{u}, t_{start}).$$

Translated-Gamma Correction

$$\hat{L}_{sig,corr} = \mathbf{b} \odot \hat{L}^a - \mathbf{c}, \quad \text{where}$$

a , \mathbf{b} and \mathbf{c} are correction parameters.

Novel View Synthesis Results

Table 1: Upper bound performance without event motion blur

Method	PSNR ↑	SSIM ↑	LPIPS ↓
E2VID + NeRF	19.49	0.847	0.268
Robust e-NeRF	28.48	0.944	0.054
Deblur e-NeRF	29.43	0.953	0.043

Table 2: Quantitative results of the real exps.

Method	08_peanuts_running			11_all_characters		
	PSNR ↑	SSIM ↑	LPIPS ↓	PSNR ↑	SSIM ↑	LPIPS ↓
E2VID + NeRF	14.85	0.690	0.595	13.12	0.695	0.627
Robust e-NeRF	18.00	0.677	0.507	15.91	0.677	0.552
Deblur e-NeRF	18.27	0.695	0.503	16.53	0.710	0.511

Table 3: Effect of camera speed. †Trained with 1/8× the batch size of baselines.

Method	$v = 0.125 \times$			$v = 1 \times$			$v = 4 \times$		
	PSNR ↑	SSIM ↑	LPIPS ↓	PSNR ↑	SSIM ↑	LPIPS ↓	PSNR ↑	SSIM ↑	LPIPS ↓
E2VID + NeRF	18.58	0.849	0.259	18.85	0.839	0.278	17.82	0.804	0.328
Robust e-NeRF	28.31	0.943	0.050	26.11	0.924	0.074	22.18	0.861	0.122
Deblur e-NeRF†	28.71	0.948	0.048	28.41	0.947	0.049	27.48	0.939	0.061

Table 4: Effect of scene illuminance. †Trained with 1/8× the batch size of baselines.

Method	$E_{sc} = 100\,000\,lux$			$E_{sc} = 1\,000\,lux$			$E_{sc} = 10\,lux$		
	PSNR ↑	SSIM ↑	LPIPS ↓	PSNR ↑	SSIM ↑	LPIPS ↓	PSNR ↑	SSIM ↑	LPIPS ↓
E2VID + NeRF	19.27	0.846	0.268	18.85	0.839	0.278	17.24	0.804	0.354
Robust e-NeRF	27.62	0.942	0.055	26.11	0.924	0.074	22.72	0.870	0.129
Deblur e-NeRF†	28.73	0.948	0.047	28.41	0.947	0.049	28.62	0.935	0.059

Table 5: Collective effect of camera speed and scene illuminance. †Trained with 1/8× the batch size of baselines.

Method	Opt. C_p & τ	Opt. Ω	$v = 0.125 \times, E_{sc} = 100\,000\,lux$			$v = 1 \times, E_{sc} = 1\,000\,lux$			$v = 4 \times, E_{sc} = 10\,lux$		
			PSNR ↑	SSIM ↑	LPIPS ↓	PSNR ↑	SSIM ↑	LPIPS ↓	PSNR ↑	SSIM ↑	LPIPS ↓
E2VID + NeRF	—	—	19.19	0.844	0.281	18.85	0.839	0.278	15.37	0.799	0.436
Robust e-NeRF	×	—	28.27	0.944	0.057	26.11	0.924	0.074	18.42	0.814	0.255
	✓	—	28.28	0.944	0.051	26.31	0.923	0.075	18.51	0.812	0.254
Deblur e-NeRF†	×	×	29.00	0.950	0.043	28.41	0.947	0.049	26.15	0.904	0.134
	×	✓	28.19	0.943	0.046	26.07	0.930	0.067	25.59	0.896	0.156

